

AProVE

20th International Workshop on Termination

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AProVE: Becoming Open Source and Recent Improvements



[AProVE](#)

[Web Interface](#)

[Download](#)

[References](#)

[Contributors](#)

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AUTOMATED PROGRAM VERIFICATION ENVIRONMENT WEB INTERFACE

AProVE is a system for automated termination and complexity proofs of term rewrite systems (TRSs) and several variations of TRSs. Moreover, AProVE also handles several other formalisms, e.g., imperative programs (Java Bytecode and C / LLVM), functional programs (Haskell 98), and logic programs (Prolog). The power of AProVE is demonstrated in the annual [International Competition of Termination Tools](#) and the [International Competition on Software Verification](#). AProVE also won two Kurt Gödel medals at VSL 2014.

There are two possibilities to use AProVE:

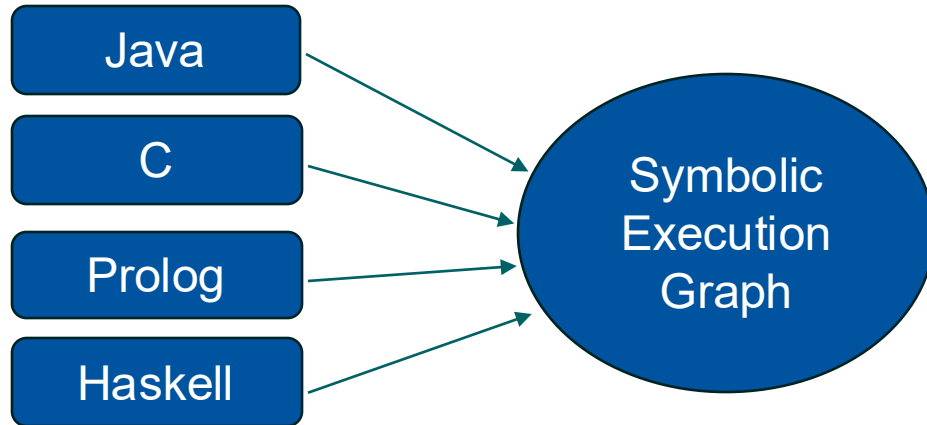
- [Web Interface](#): This web interface runs AProVE directly via the web on a virtual machine assigned eight cores of a Broadwell CPU. The web interface uses Docker containers to isolate the AProVE instances.
- [Download](#): You can download the full version of AProVE.

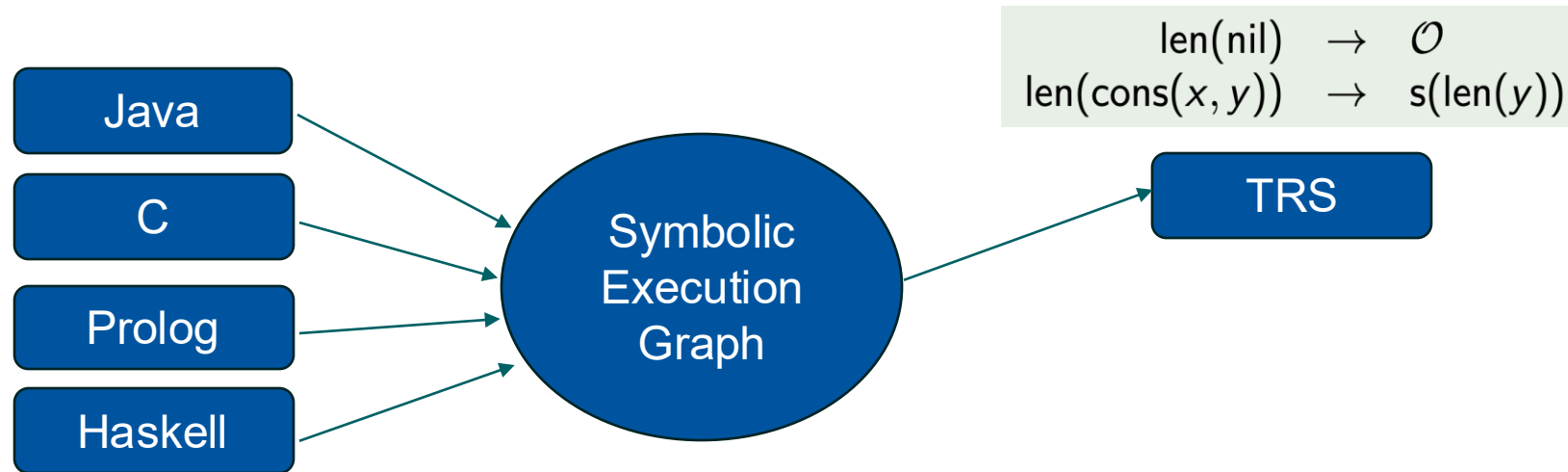
Java

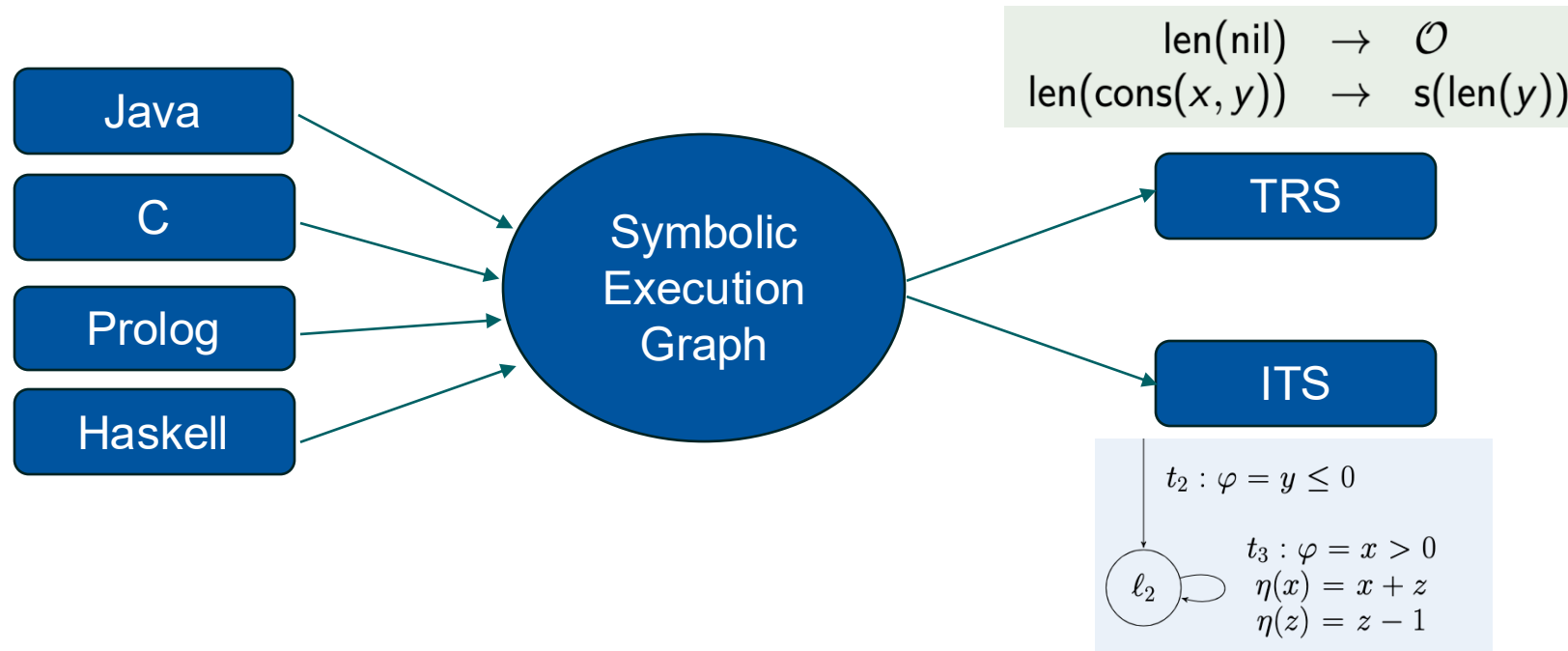
C

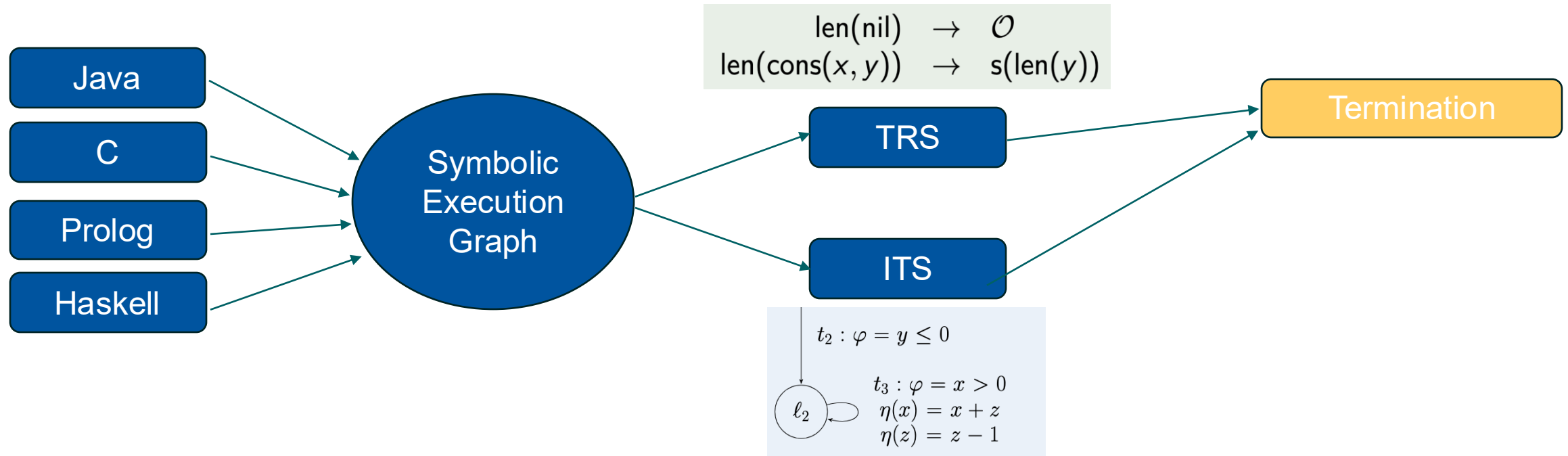
Prolog

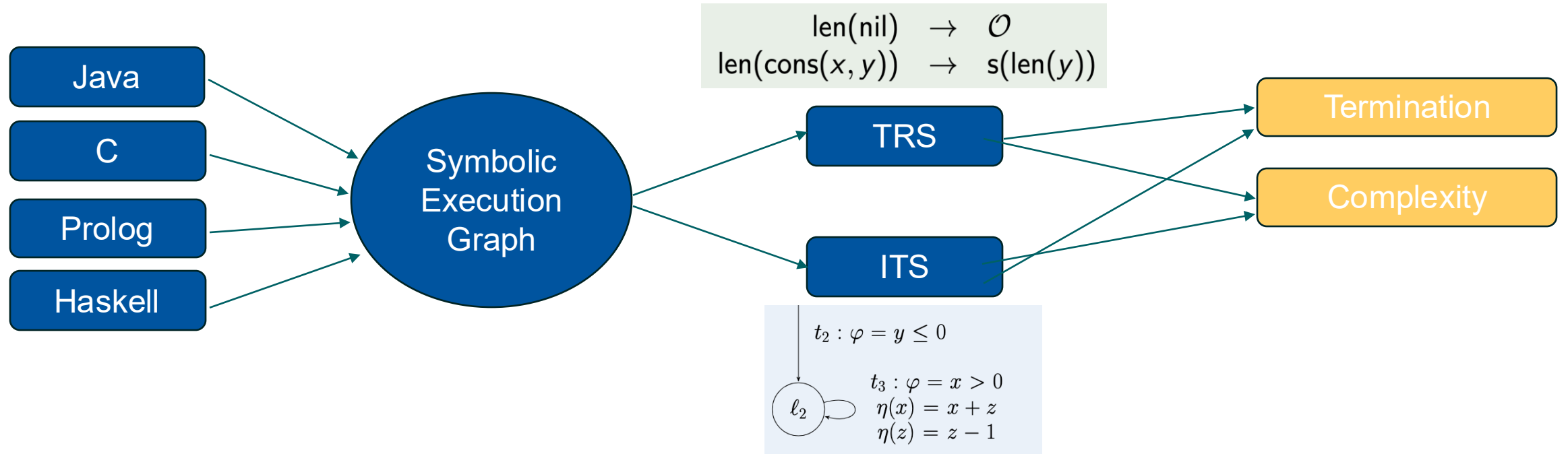
Haskell

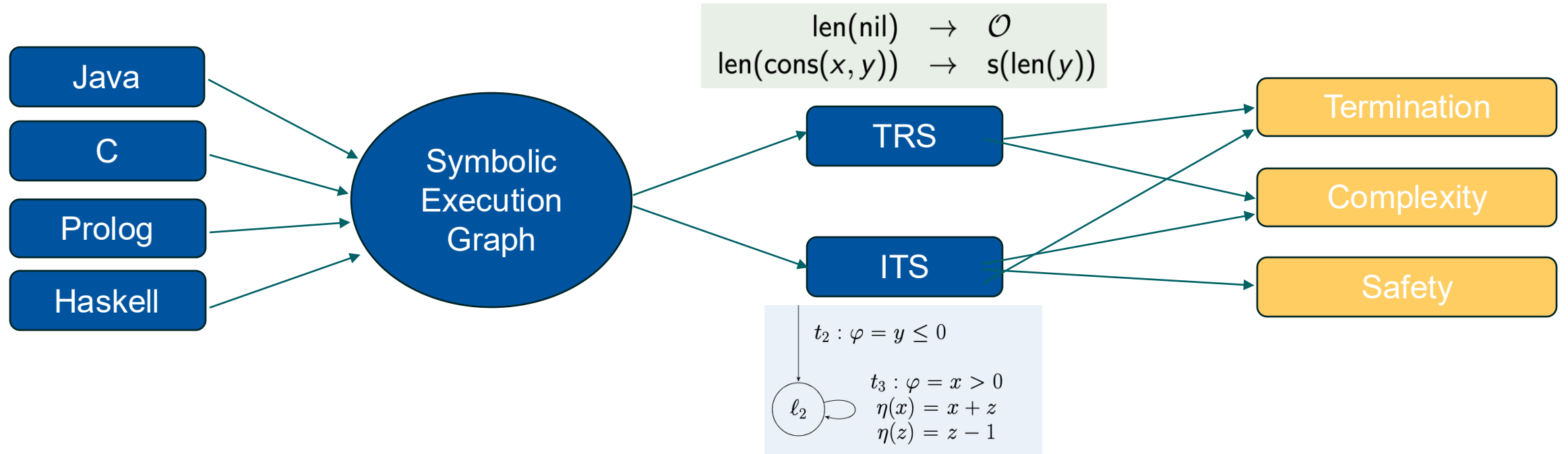


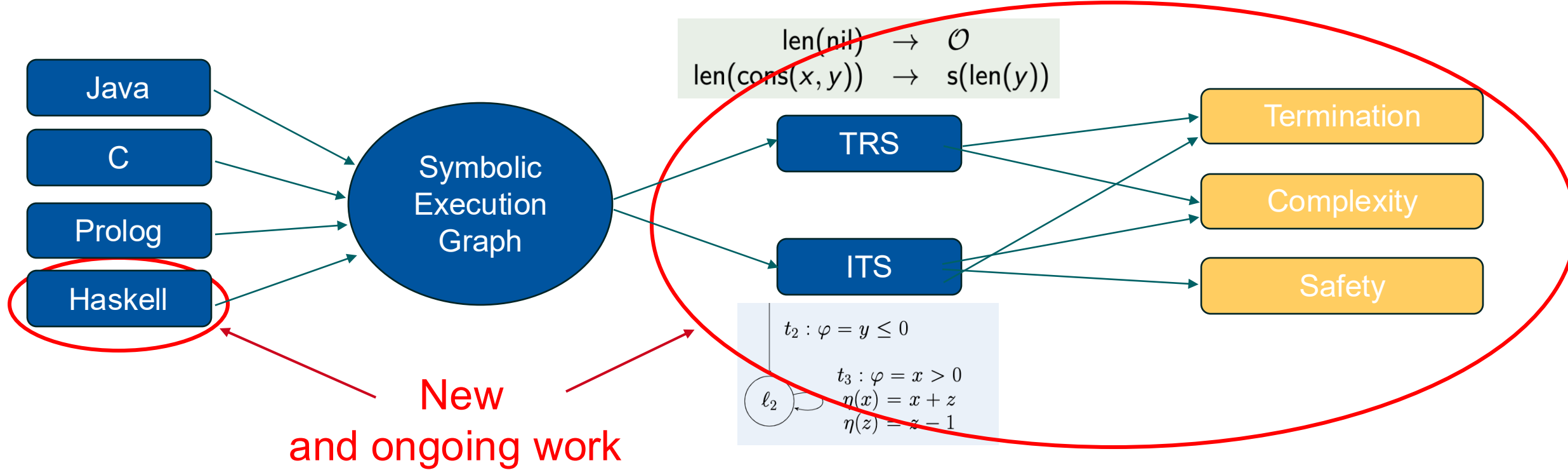


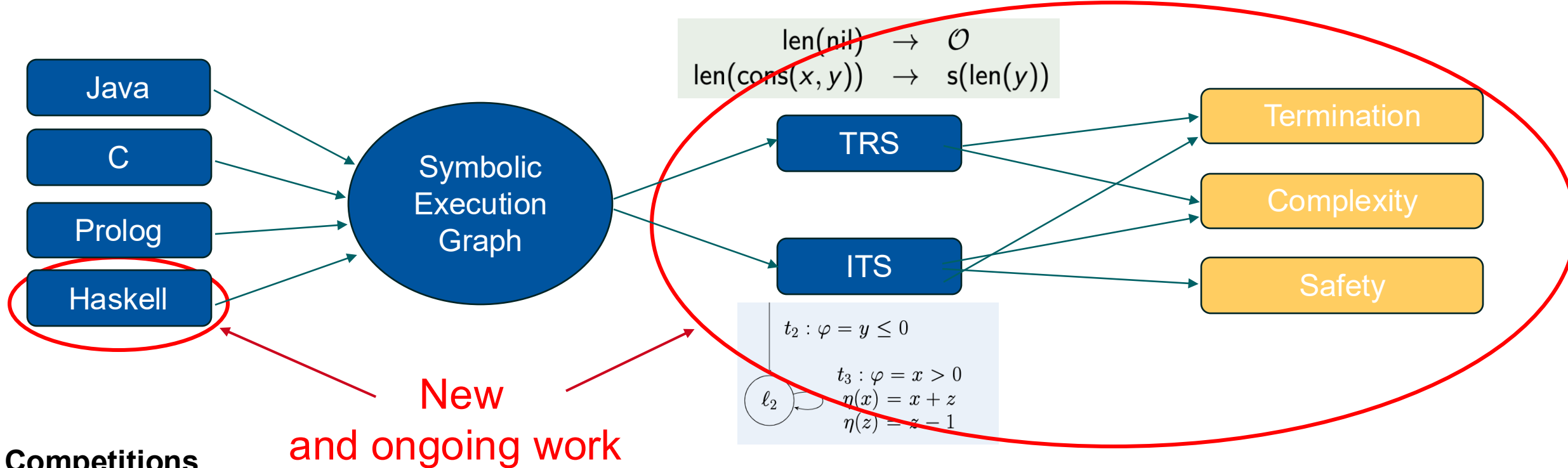






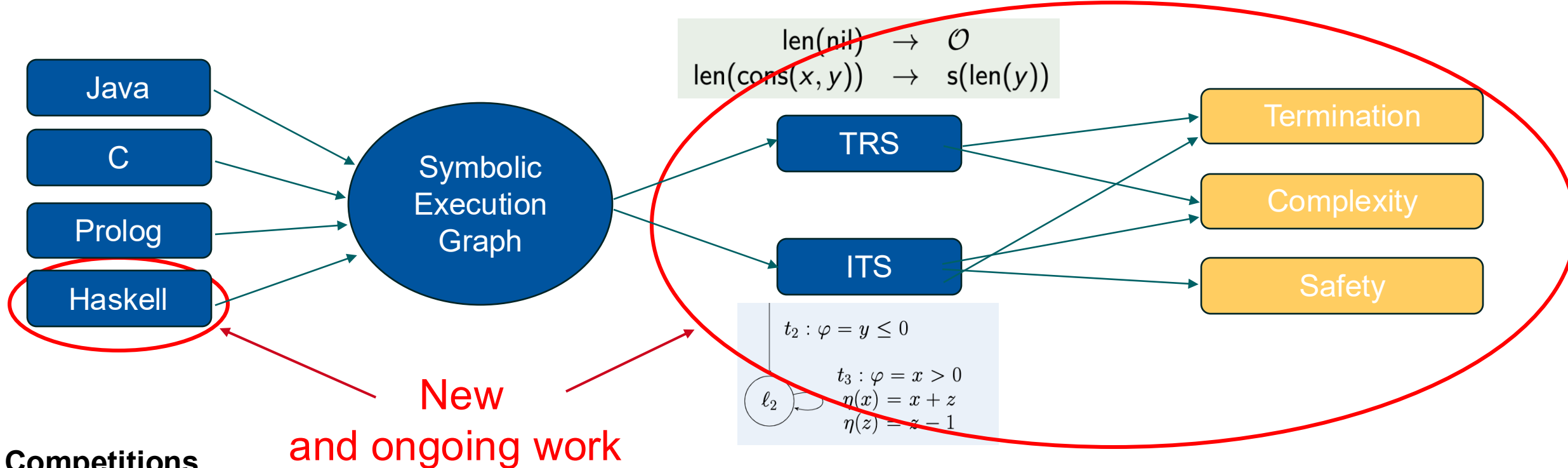






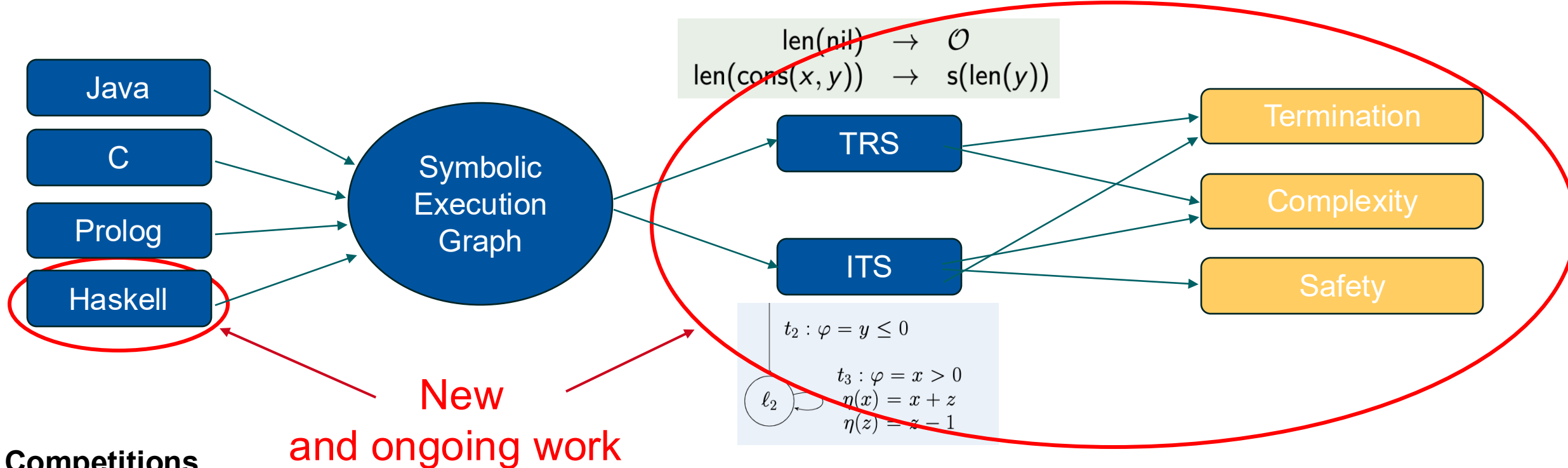
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 - Participation in nearly all categories (TRS-Standard, TRS-Relative, Java, C, PTRS-Standard, ITS, etc.)



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- Confluence Competition (First Time!)
 - Participation in the TRS category for confluence analysis.

Complexity of TRSs

$$\begin{array}{lcl} \text{plus}(\mathcal{O}, y) & \rightarrow & y \\ \text{plus}(s(x), y) & \rightarrow & s(\text{plus}(x, y)) \end{array}$$

Derivational Complexity

Runtime Complexity

Complexity of TRSs

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\mathcal{R}

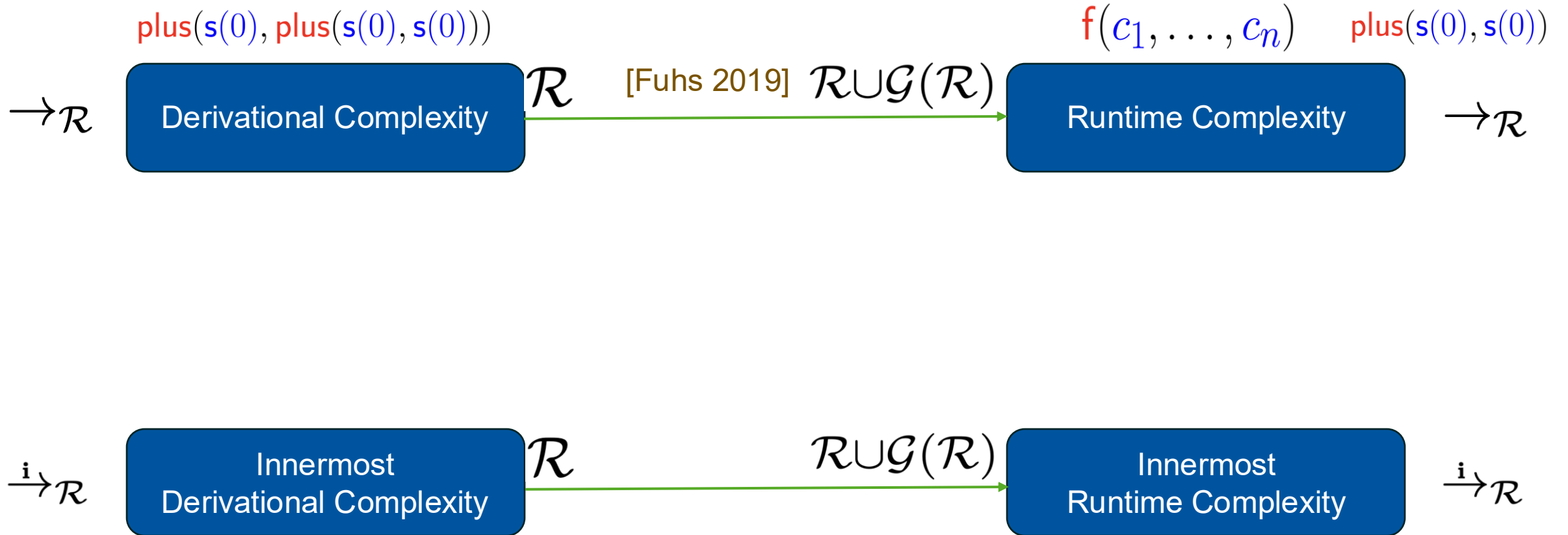
[Fuhs 2019] $\mathcal{RUG}(\mathcal{R})$

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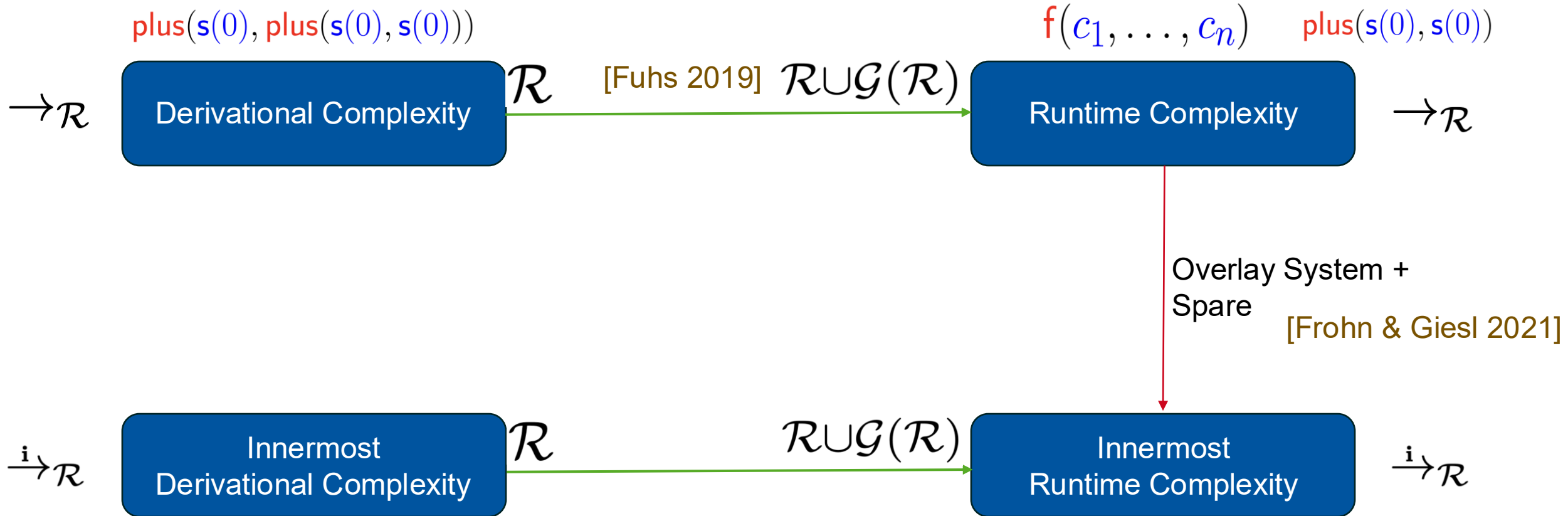
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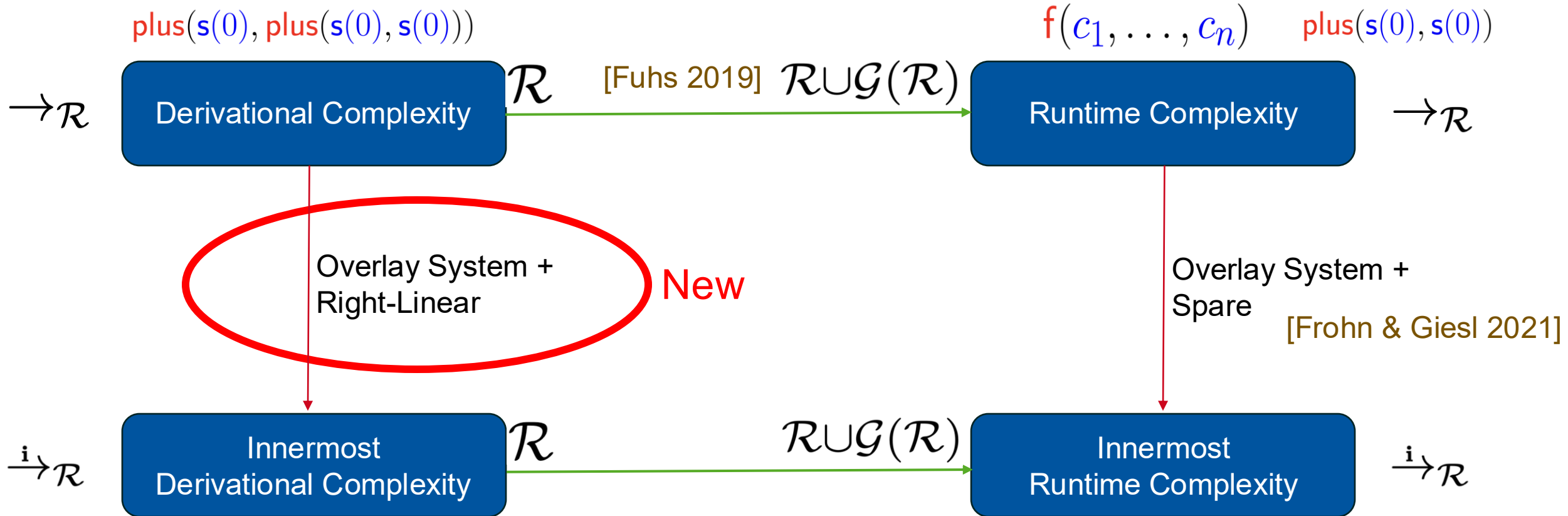
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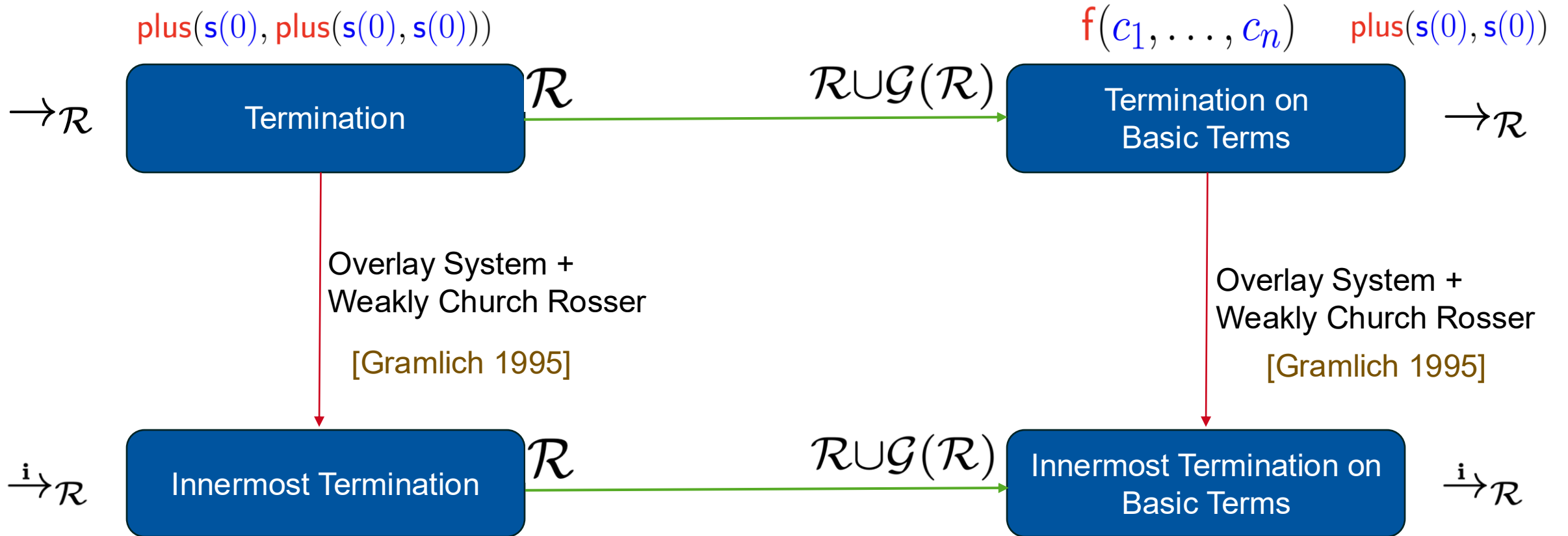
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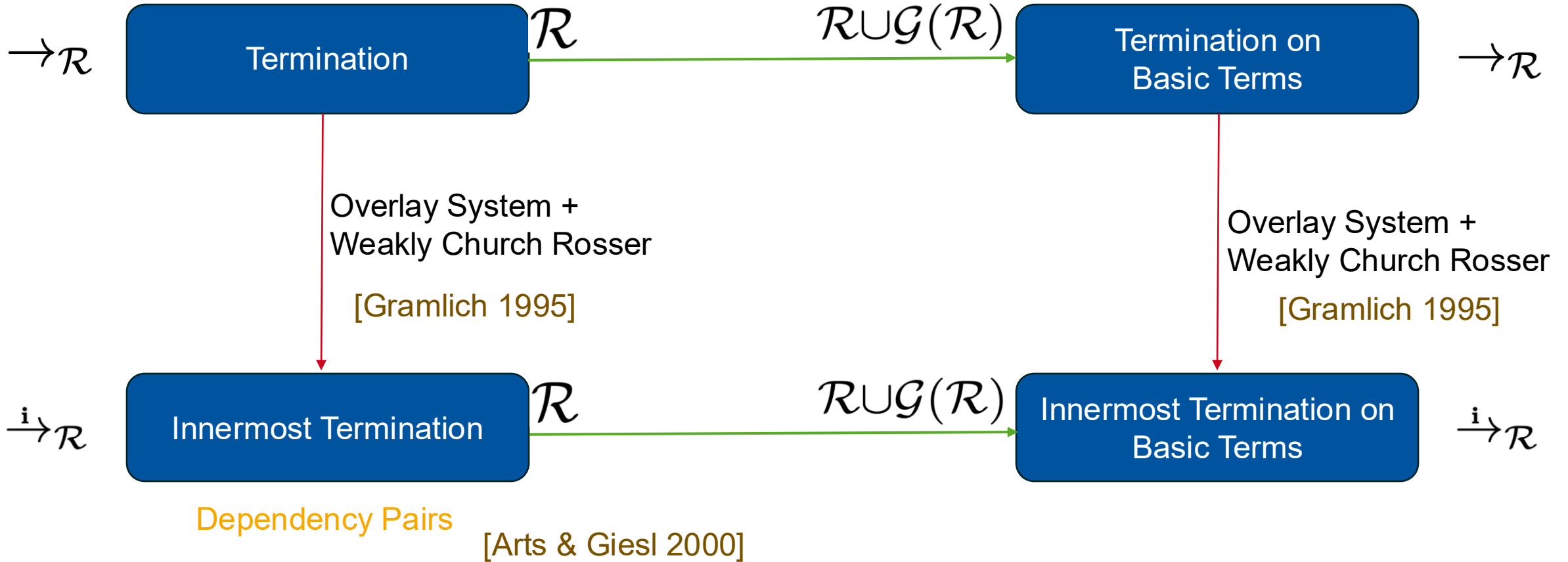
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Dependency Pairs [Arts & Giesl 2000]

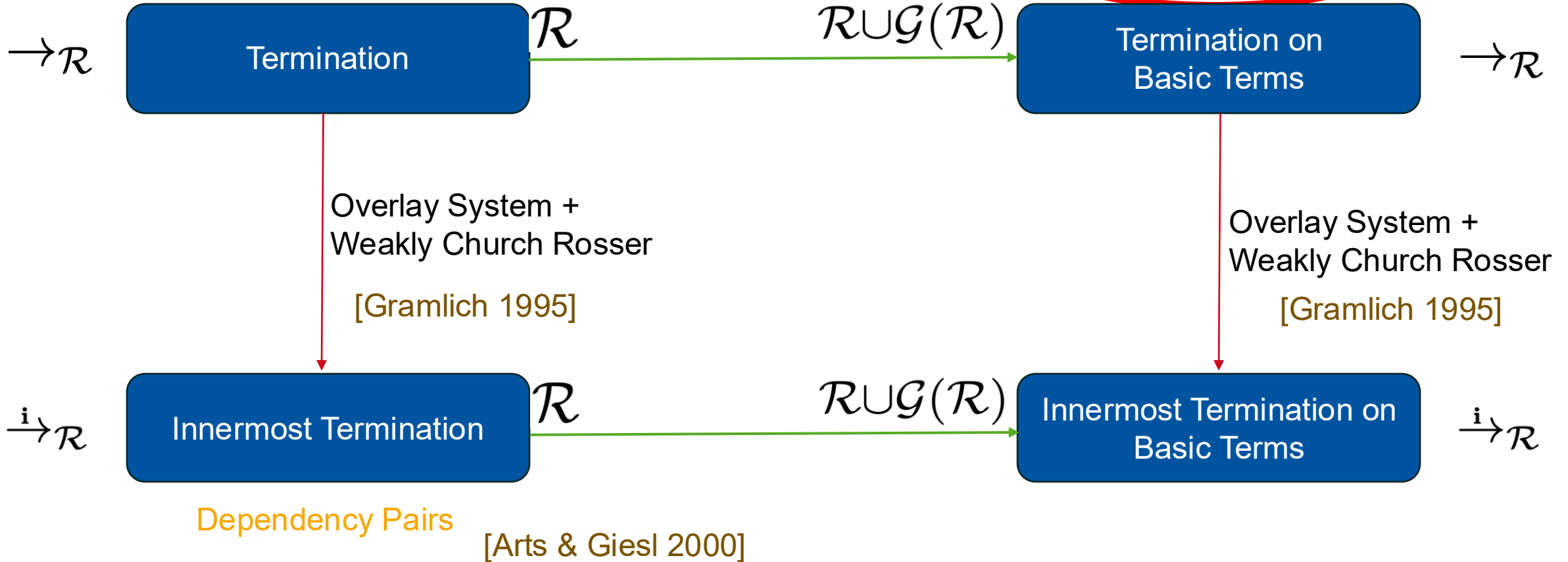


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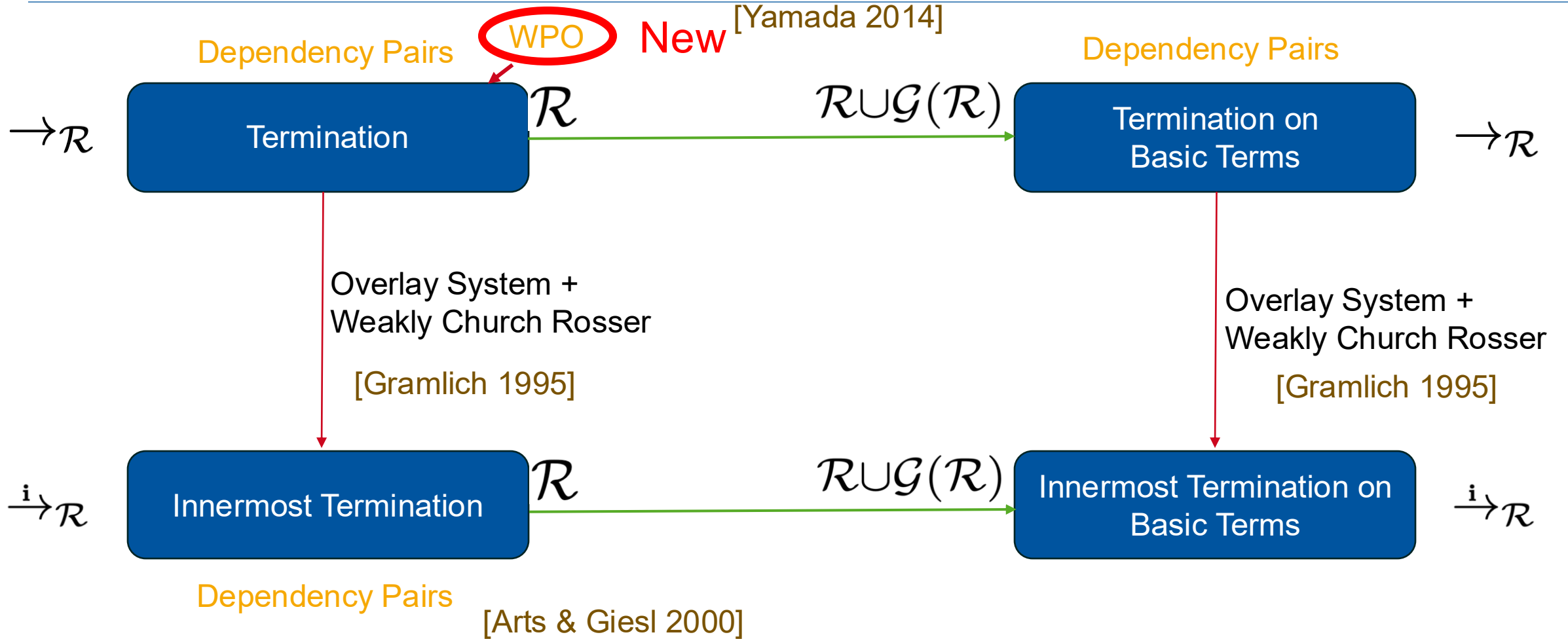
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$$g \rightarrow \{1/2 : 0, 1/2 : g\}$$

 $\rightarrow_{\mathcal{R}}$

AST

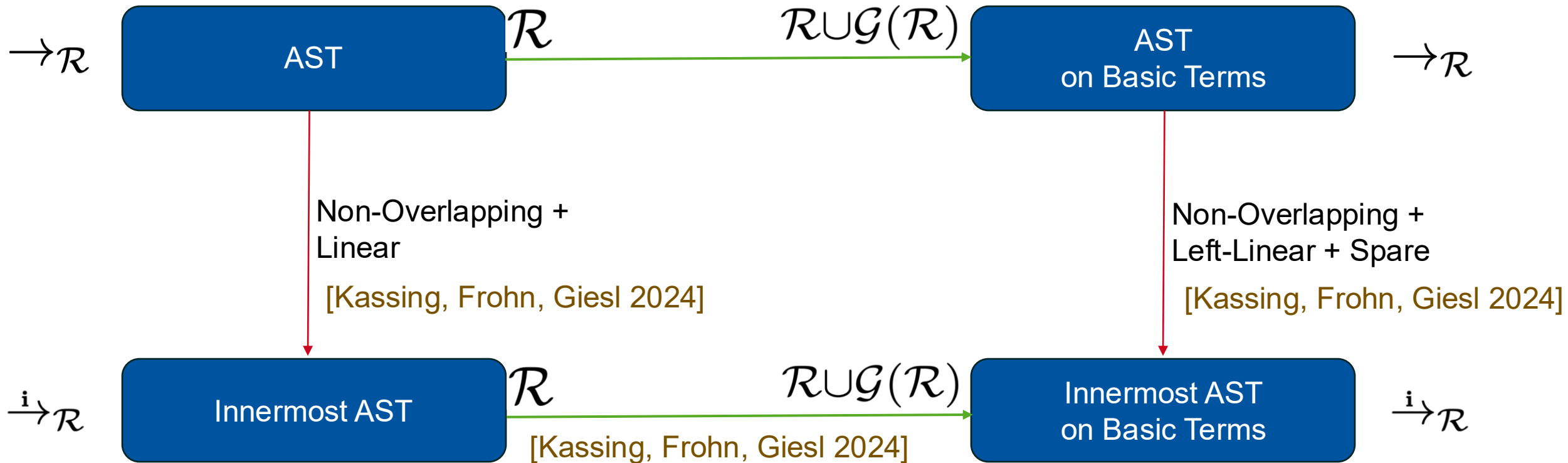
AST
on Basic Terms $\rightarrow_{\mathcal{R}}$ $\xrightarrow{i}_{\mathcal{R}}$

Innermost AST

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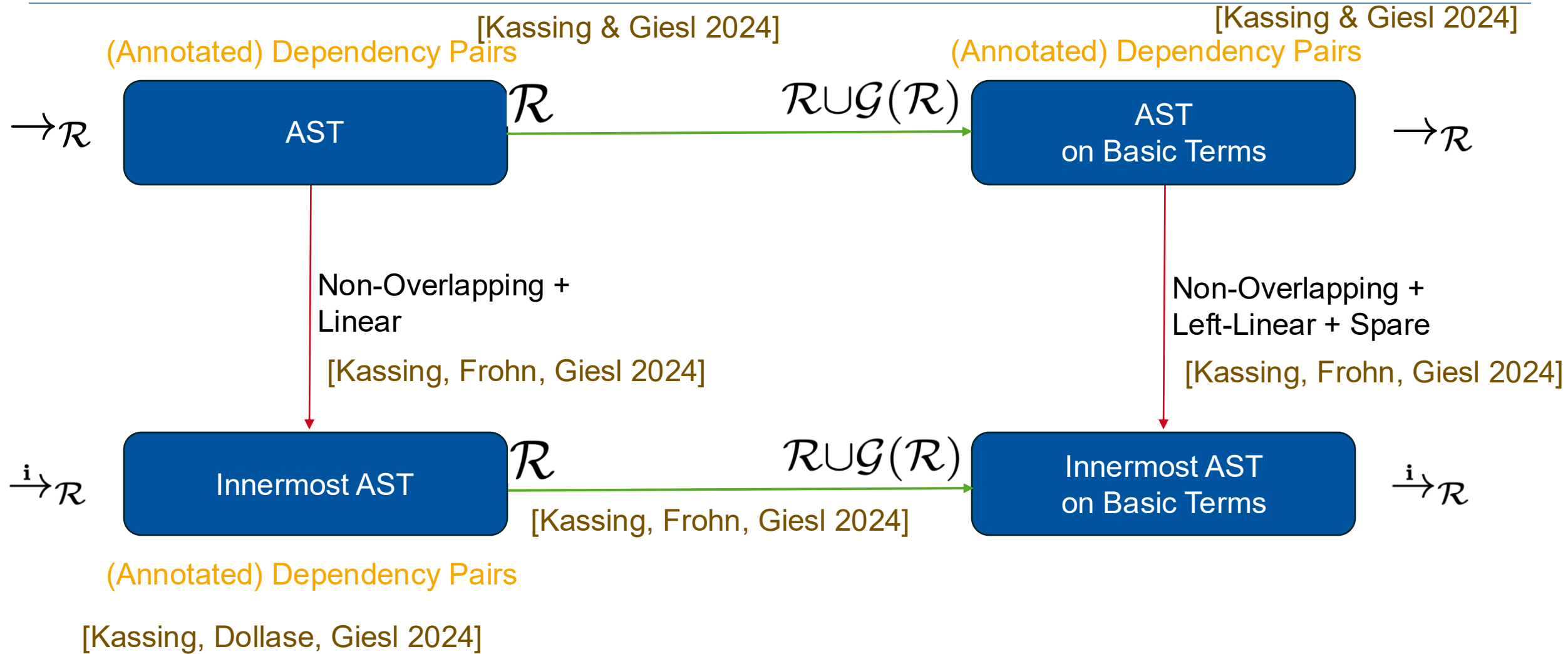
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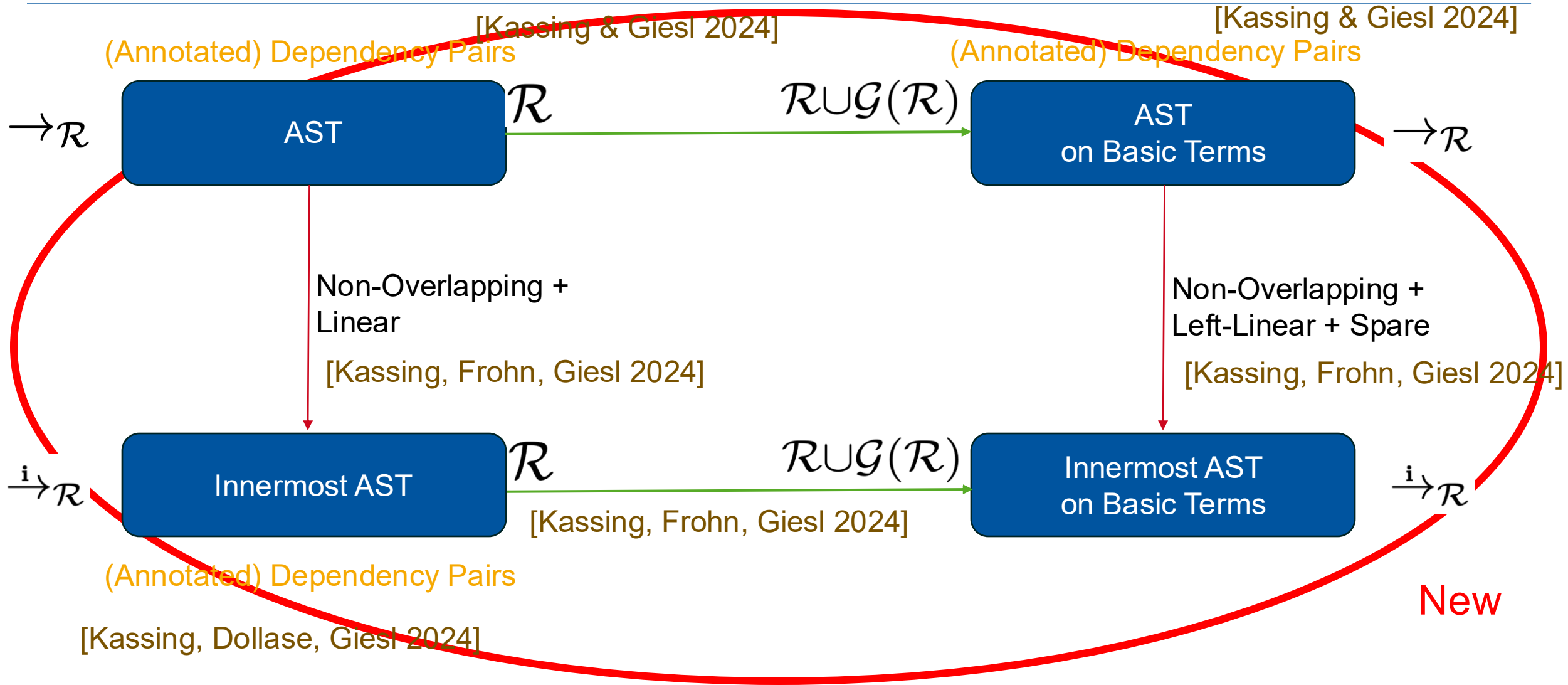
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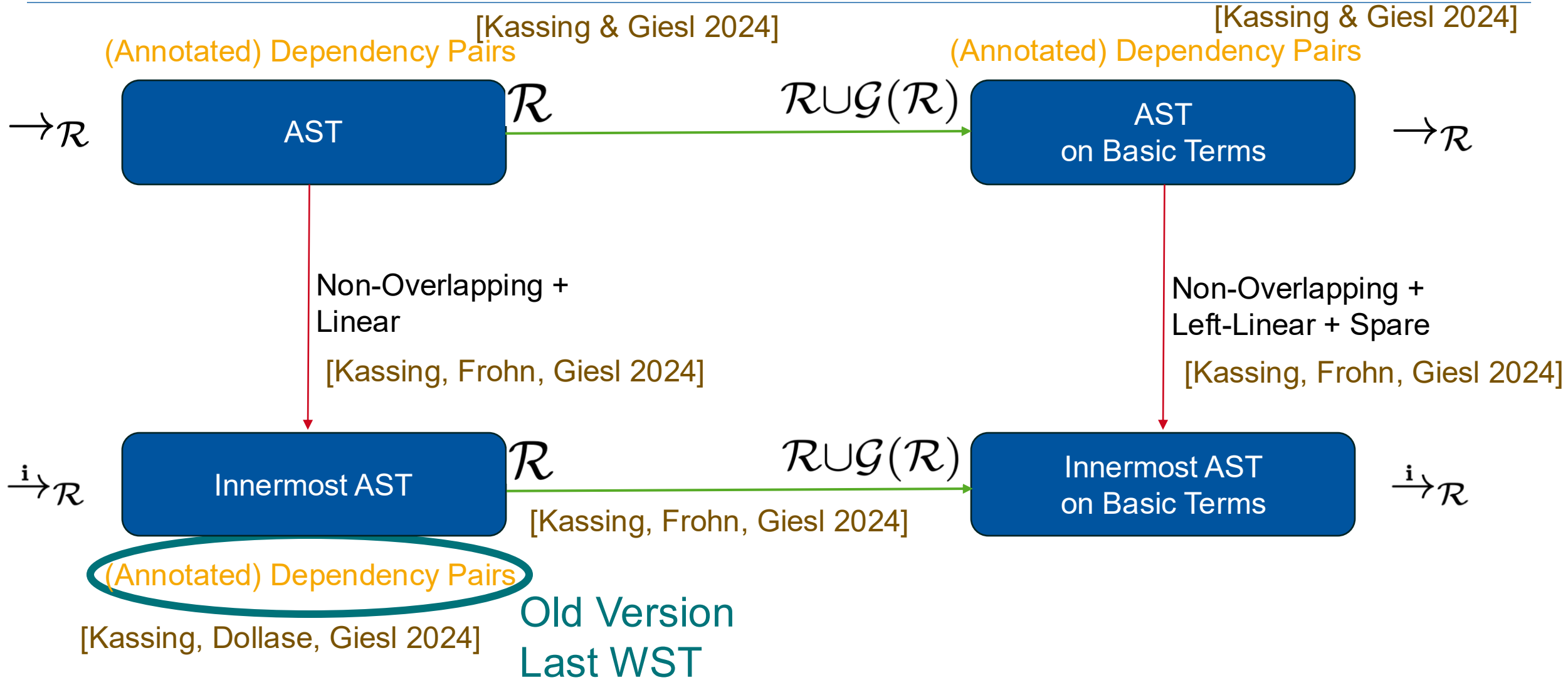
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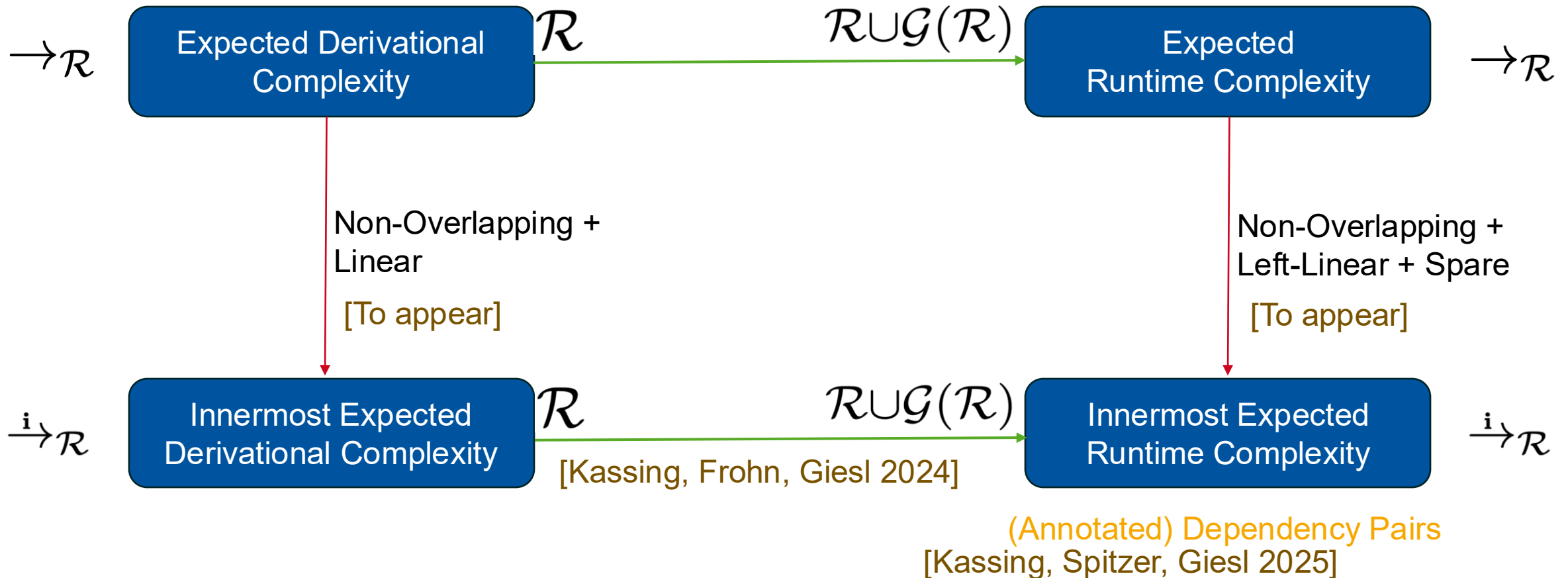
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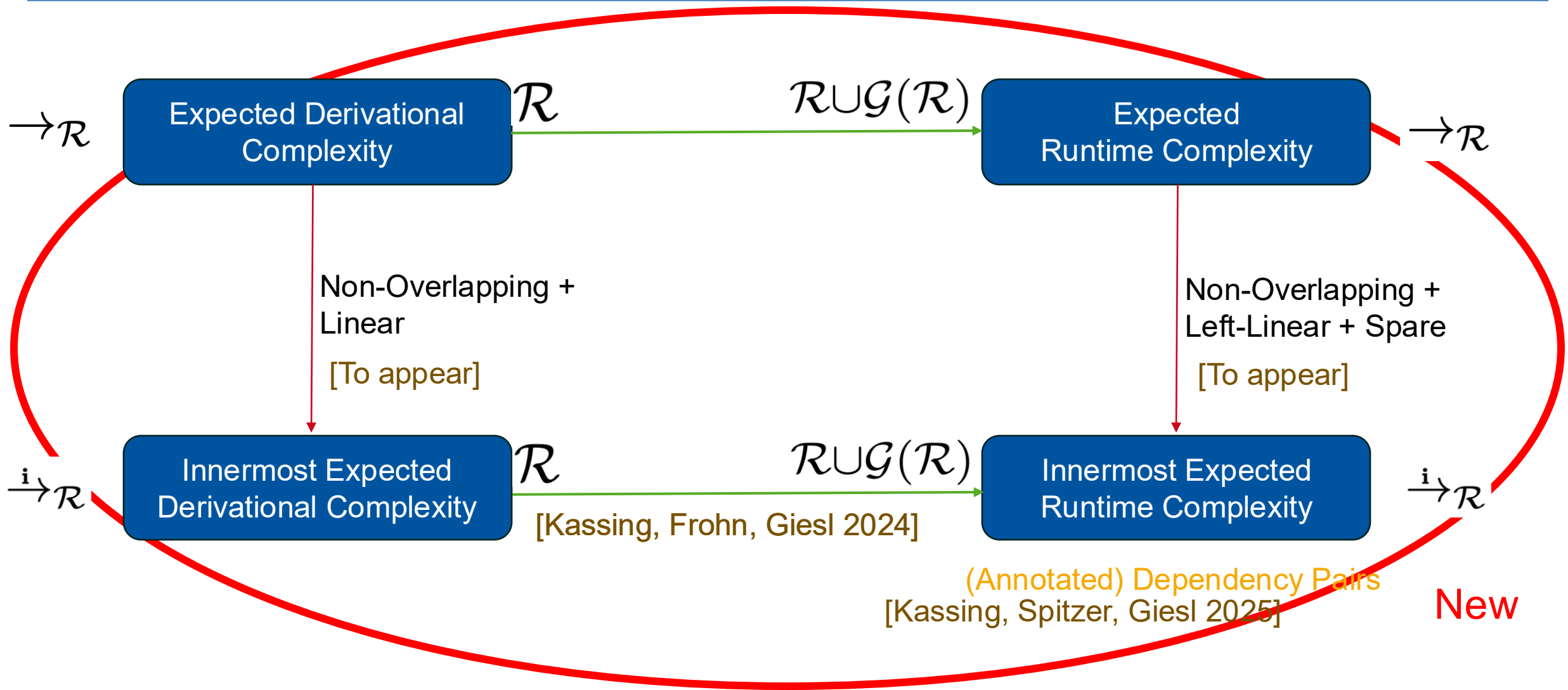
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Everything New:

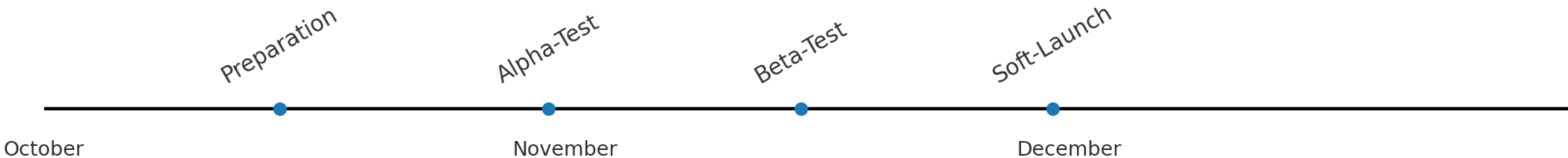
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 - Implemented WPO
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 - Properties to Move From Derivational Complexity to Innermost Derivational Complexity
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 - (Annotated) Dependency Pairs [IJCAR'24]
- **Probabilistic TRS:**
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 - (Annotated) Dependency Pairs for Expected Complexity and SAST [PPDP'25]
 - From Innermost to Full Rewriting for AST, SAST, and Expected Complexity [FoSSaCS'24]
 - Modularity Results for AST/PAST/SAST [To appear]
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Open Source Release

Open Source Release Timeline (End of 2025)



Target License: **LGPL (Lesser General Public License)**

- You can **use, modify, and redistribute** LGPL software (for free or commercially).
- If you **modify the LGPL-covered code itself**, you must release those modifications under the LGPL.
- If you **just use the library** (e.g., link to it in your own code), your own program does *not* have to be LGPL/GPL.

Future Work / Current Research / Miscellaneous

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 - **Disproving** AST, PAST, or SAST
 - Subclasses of PTRS, where AST, PAST, or SAST is **Decidable**
 - **Reachability** Probability in PTRSs
 - Combining PTRSs with Natural Numbers (**LCPTRSs?**)
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If you are interested in one of these topics, feel free to talk to me!

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